



# Thermal expansion in lithium manganese oxide spinels $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$ with $0 \leq x \leq 1/3$

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## HIGHLIGHTS

- The coefficients of thermal expansion in  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  with  $0 \leq x \leq 1/3$  are examined.
- The coefficients of thermal expansion in  $x = 0$  are very different between the orthorhombic axes.
- The coefficients of thermal expansion are almost independent on  $x$  at  $x \geq 0.05$ .

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## ABSTRACT

In order to know the coefficients of thermal expansion in lithium manganese oxide spinels  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  with  $0 \leq x \leq 1/3$ , X-ray diffraction measurements are performed in the temperature ( $T$ ) range from 400 to 100 K. The crystal structure for  $x = 0$  changes from the high- $T$  cubic phase ( $Fd\bar{3}m$ ) into the low- $T$  orthorhombic phase ( $Fddd$ ) below 285 K due to a cooperative the Jahn–Teller transition. Hence, the average coefficients of linear thermal expansion ( $\alpha_L$ ) in  $x = 0$  are very different between the three orthorhombic axes;  $\alpha_L = 1.3(1) \times 10^{-6} \text{ K}^{-1}$  along the  $a_o$ -axis,  $\alpha_L = 13.1(1) \times 10^{-6} \text{ K}^{-1}$  along the  $b_o$ -axis, and  $\alpha_L = 5.7(1) \times 10^{-6} \text{ K}^{-1}$  along the  $c_o$ -axis, where  $a_o$ ,  $b_o$ , and  $c_o$  are the lattice parameters of orthorhombic phase. On the other hand, the crystal structure for the samples with  $x \geq 0.05$  keeps the cubic phase ( $Fd\bar{3}m$ ) down to 100 K. The  $\alpha_L$  value is almost independent on  $x$  at  $x \geq 0.05$ , i.e.  $\alpha_L \sim 7.0 \times 10^{-6} \text{ K}^{-1}$ . This suggests that the bond strength between Mn(Li) and  $\text{O}^{2-}$  ions does not increase by the partial substitution of Li ions for Mn ions.

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## 1. Introduction

Due to increasing demand for secondary batteries with high energy density and long cycle-life, lithium-ion battery (LIB) has been heavily investigated over the past decade [1]. Although a liquid electrolyte consisted of lithium salt and organic solvents is used in the current commercial LIB, all solid-state LIB having a solid electrolyte is considered to be a next-generation battery. This is because one can increase the energy density of LIB by applying three-dimensional battery architectures [2]. Moreover, the side reactions leading to capacity fading are suppressed compared to the conventional LIB [3].

One of the biggest issues in realizing all solid-state LIB is how to construct the solid–solid interfaces. Lithium insertion materials such as  $\text{LiCoO}_2$  [4–7],  $\text{LiNiO}_2$  [8,9], etc. maintain these framework structures during the charge and discharge reactions. The

extraction/insertion of lithium ions, however, induces the change in lattice parameters, namely, the change in lattice volume ( $\Delta V$ ), except for so-called zero-strain insertion material  $\text{Li}[\text{Li}_{1/3}\text{Ti}_{5/3}]\text{O}_4$  [10]. Considering the application in the wide temperature ( $T$ ) range above 100 K, not only the  $\Delta V$  value, but also the coefficient of thermal expansion (CTE) in lithium insertion material is crucial information for constructing the solid–solid interfaces. Here, the thermal expansion in materials is explained by introducing the anharmonicity of lattice vibration to the interatomic potential energy [11,12]. Thus, the CTE would also provide an indicator of bond strength between atoms of lithium insertion materials as in the case for a large number of glasses, metals, and oxides [13]. Indeed, our recent X-ray diffraction (XRD) studies on  $\text{Li}_y\text{CoO}_2$  indicate the anisotropic thermal expansion between the interplane and intraplane of the  $\text{CoO}_2$  layer, suggesting a rigid network of edge-sharing  $\text{CoO}_6$  octahedra. [7].

Lithium manganese oxide  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  (LMO) with  $0 \leq x \leq 1/3$  adopts the cubic spinel structure with  $Fd\bar{3}m$  space group at room  $T$  [14–16], and consequently, shows smaller  $\Delta V$  value than  $\text{LiCoO}_2$  [5–7] and  $\text{LiNiO}_2$  [9]. LMO is, hence, thought to be a suitable

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electrode material for all solid-state LIB. According to the previous structural analyses on LMO, LMO with  $x = 0$  exhibits a structural phase transition from high- $T$  cubic ( $Fd\bar{3}m$ ) phase to low- $T$  tetragonal ( $I4_1amd$ ) [17,18] phase or orthorhombic ( $Fddd$ ) [19–21] phase at around 285 K. Furthermore, LMO with  $x = 1/3$  contains small amount of  $\text{Li}_2\text{MnO}_3$  impurity [22–24]. On the electrochemical tests, LMO with  $x = 0$  shows poor cycle performance even at room  $T$  [16,25,26], while LMO with  $x \geq 0.05$  shows relatively stable cycle life at room  $T$  [25–28]. Despite of the extensive studies on LMO, the coefficients of linear thermal expansion ( $\alpha_L$ ) and volumetric thermal expansion ( $\beta_V$ ) of LMO are still unknown. We have, therefore, performed a systematic XRD study on LMO in the  $T$  range 400 to 100 K, in order to know both  $T$  dependence of lattice parameters and  $x$  dependence of CTE. In this paper, we report the  $\alpha_L$  and  $\beta_V$  for LMO together with those for other lithium insertion materials.

## 2. Experimental

Powder samples of LMO with  $x = 0, 0.05, 0.1, 0.15, 0.2$ , and  $1/3$  were prepared by a two-step solid-state reaction technique [24,27] in order to obtain highly crystallized LMO samples. The reaction mixture of  $\text{LiOH} \cdot \text{H}_2\text{O}$  and  $\text{MnO}_2$  was well mixed with a mortar and pestle, and pressed into a pellet of 23 mm diameter and  $\sim 5$  mm thickness. The pellet was heated at 1273 K in air for 12 h, then the obtained powder was crushed and repressed into a pellet again, and finally the pellet was oxidized at 1073 K for 24 h, 923 K for 24 h, 873 K for 24 h, 823 K for 48 h, and 773 K for 48 h in air without cooling down to room  $T$ .

The electrochemical reactivity for LMO was examined in a nonaqueous lithium cell. In preparing the electrode, polyvinylidene fluoride (PVdF) dissolved in  $N$ -methyl-2-pyrrolidone solution was used as a binder. The black viscous slurry consisting of 88 wt% LMO powder, 6 wt% acetylene black, and 6 wt% PVdF was cast on an aluminum foil with blade. The electrode ( $\phi$  16 mm) was dried under vacuum at 393 K for 12 h. The lithium metal sheet pressed on a stainless steel plate ( $\phi$  19 mm) was used as a counter electrode. Two sheets of porous polyethylene membrane (Tonen-General Sekiyu K. K., Japan) were used as a separator. The electrolyte was 1 M  $\text{LiPF}_6$  dissolved in ethylene carbonate (EC)/dimethyl carbonate (DEC) (1/1 volume ratio) solution (Kishida Chemical Co. Ltd., Japan).

XRD measurements were carried out in the  $T$  range from 400 to 100 K at a synchrotron radiation facility of SPring-8 (BL19B2). For the  $x = 0$  sample, XRD measurements were also made in the  $T$  range from 287.5 to 275 K. After reaching the every setting  $T$ , we took the waiting time for 3 min to stabilize the  $T$  of the sample. The  $T$  of the sample during the XRD measurements was controlled by a continuous  $\text{N}_2$ -flow device (CGD-1, Rigaku Co. Ltd., Japan) with a precision of  $\pm 0.1$  K. The wavelength of the X-ray was estimated as  $0.70000(1)$  Å by the XRD measurements on NIST  $\text{CeO}_2$  standard (674a). All the LMO samples were packed into a boro-silicate glass capillary tube with 0.3 mm diameter. The Rietveld analyses were performed by RIETAN2000 [29].

## 3. Results

### 3.1. XRD patterns of $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$

Fig. 1 shows the XRD patterns of the LMO samples with (a)  $x = 0$ , (b)  $x = 0.1$ , (c)  $x = 0.2$ , and (d)  $x = 1/3$  at 400 K. The XRD patterns for the  $x = 0, 0.1$ , and  $0.2$  samples are identified as a single phase of the spinel structure with space group of  $Fd\bar{3}m$ , in which  $\text{Li}^+$  ions occupy both the tetrahedral  $8a$  and octahedral  $16d$  sites and Mn ions sit the octahedral  $16d$  site. On the contrary, for the  $x = 1/3$  sample, the

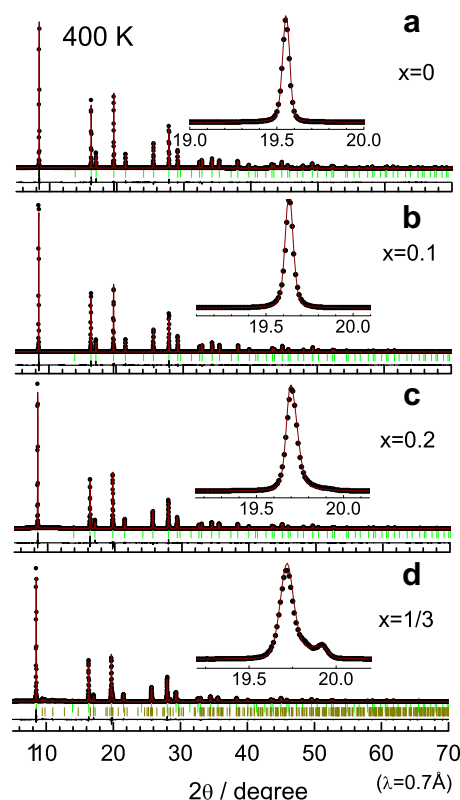


Fig. 1. XRD patterns of the  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  samples with (a)  $x = 0$ , (b)  $x = 0.1$ , (c)  $x = 0.2$ , and (d)  $x = 1/3$  at 400 K. The enlarged diffraction line (major diffraction line) in the inset corresponds to the 400 diffraction line of the cubic spinel structure.

weak diffraction lines are observed in the higher diffraction angle in the vicinity of the major diffraction lines. This is clearly understood by the enlarged diffraction line around  $2\theta = 20^\circ$  (see the inset in Fig. 1 (d)). According to the previous studies on  $\text{Li}[\text{Li}_{1/3}\text{Mn}_{5/3}]\text{O}_4$  [22–24], the  $\text{Li}_2\text{MnO}_3$  impurity with a monoclinic ( $C2/m$ ) structure inevitably coexists in the sample due to the extremely slow reaction rate of  $(1-x)\text{LiMn}_2\text{O}_4 + x\text{Li}_2\text{MnO}_3 + x/2\text{O}_2 \rightarrow \text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$ . The XRD pattern for the  $x = 1/3$  sample is, thus, assigned as a mixture of the spinel phase ( $Fd\bar{3}m$ ) and the  $\text{Li}_2\text{MnO}_3$  phase ( $C2/m$ ). The weight fraction of the  $\text{Li}_2\text{MnO}_3$  phase [ $W(\text{Li}_2\text{MnO}_3)$ ] in the  $x = 1/3$  sample is estimated to be  $\sim 0.11$  by following equation:

$$W_p = S_p(ZMV)_p / \sum_{i=1}^n S_i(ZMV)_i, \quad (1)$$

where  $W$  is the relative weight fraction of the phase  $p$  in a mixture of the  $n$  phase,  $S$  the Rietveld scale factor,  $Z$  the number of formula units per unit cell,  $M$  the mass of the formula unit, and  $V$  the unit cell volume, respectively. The XRD patterns at 300 K (not shown) are essentially the same to those at 400 K; the XRD patterns for  $x \leq 0.2$  are assigned as the single spinel phase ( $Fd\bar{3}m$ ), while the XRD pattern for  $x = 1/3$  is assigned as the mixture of the spinel phase ( $Fd\bar{3}m$ ) and the  $\text{Li}_2\text{MnO}_3$  phase ( $C2/m$ ).

Fig. 2 shows the XRD patterns of the  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  samples with (a)  $x = 0$ , (b)  $x = 0.1$ , (c)  $x = 0.2$ , and (d)  $x = 1/3$  at 100 K. As clearly seen in the inset of Fig. 2(a), three diffraction lines are observed around  $2\theta = 20^\circ$ , suggesting a structural phase transition below 300 K. Although the crystal structure of stoichiometric  $\text{LiMn}_2\text{O}_4$  below room  $T$  is different among the research groups [17–21], there seems to be general agreements that the onset of the structural phase

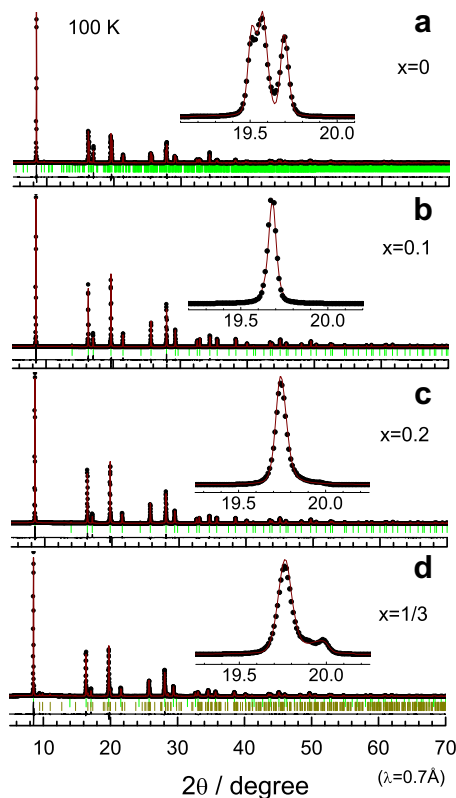


Fig. 2. XRD patterns of the  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  samples with (a)  $x = 0$ , (b)  $x = 0.1$ , (c)  $x = 0.2$ , and (d)  $x = 1/3$  at 100 K.

transition is around 280 K and that the structural phase transition is caused by the cooperative Jahn–Teller (JT) transition induced by  $\text{Mn}^{3+}$  ions with  $t_{2g}^3e_g^1$  ( $S = 2$ ). The crystal structure for the present  $x = 0$  sample at 100 K is well explained by the single orthorhombic phase ( $Fddd$ ), in which the unit cell is represented as  $3a' (=a_0) \times 3b' (=b_0) \times c' (=c_0)$ , where  $a'$ ,  $b'$ , and  $c'$  are the lattice parameters of the pseudocubic spinel phase and  $a_0$ ,  $b_0$ , and  $c_0$  are those of the orthorhombic superstructure phase [19]. For the samples with  $x \geq 0.1$ , the crystal structure at 100 K is essentially the same to those at  $T > 100$  K; the cubic spinel phase ( $Fd\bar{3}m$ ) for the samples with  $x = 0.1$  and 0.2 and a mixture of cubic spinel phase ( $Fd\bar{3}m$ ) and the  $\text{Li}_2\text{MnO}_3$  phase ( $C2/m$ ) for the  $x = 1/3$  sample.

### 3.2. Electrochemical properties of $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$

Fig. 3 shows the charge and discharge curves for the  $\text{Li}/\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  cells with (a)  $x = 0$ , (b)  $x = 0.1$ , (c)  $x = 0.2$ , and (d)  $x = 1/3$ . The cells were operated in the voltage range between 3.0 and 5.0 V at current density of  $0.25 \text{ mA cm}^{-2}$  at 298 K. For the  $x = 0$  sample, the charge capacity is about  $140 \text{ mAh g}^{-1}$  at the first cycle, but decreases cycle by cycle. As described in 3.1 Section, the crystal structure for  $x = 0$  keeps the cubic spinel phase ( $Fd\bar{3}m$ ) at 300 K. Hence, the capacity fading for  $x = 0$  is attributed to the formation and disappearance of the “double hexagonal phase” [25] which corresponds to the voltage plateau around 4.5 and 3.3 V, respectively. Other contribution would come from the dissolution of Mn ions from the lattice [30,31]. The excellent cycleability is obtained for the  $x \geq 0.1$  samples, while the rechargeable capacity ( $Q_{\text{recha}}$ ) decreases with increasing  $x$ . If the  $Q_{\text{recha}}$  value for LMO is determined by the amount of  $\text{Mn}^{3+}$  ions, more correctly, the electrochemical reaction of LMO proceeds as follow,

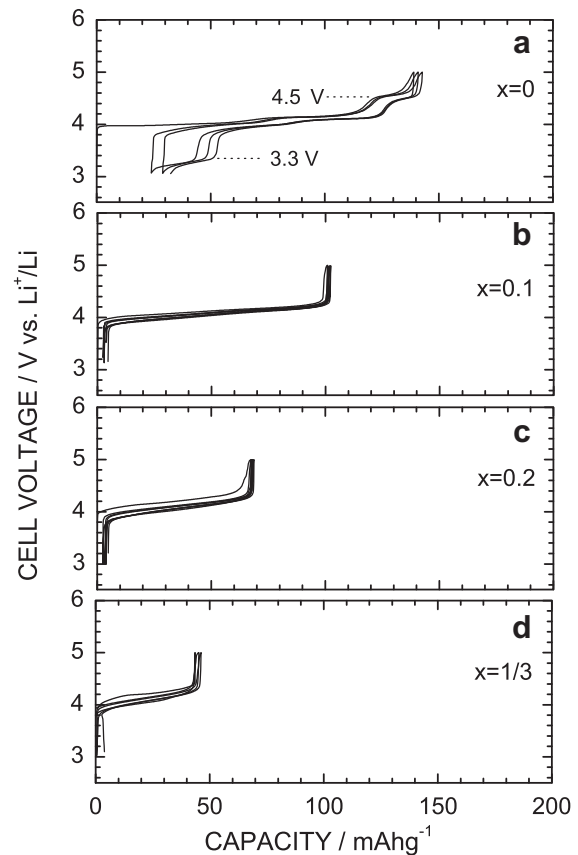
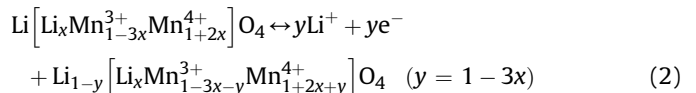


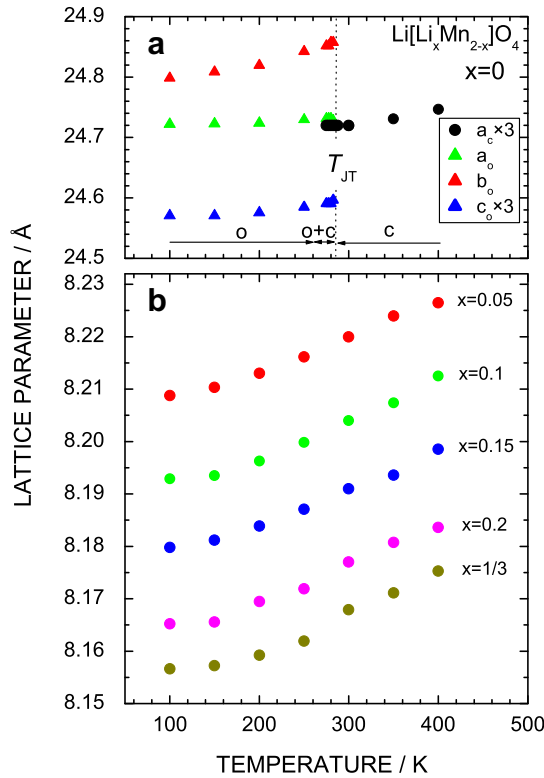
Fig. 3. Charge and discharge curves for the  $\text{Li}/\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  cells with (a)  $x = 0$ , (b)  $x = 0.1$ , (c)  $x = 0.2$ , and (d)  $x = 1/3$  operated at current density of  $0.25 \text{ mA cm}^{-2}$  at 298 K.



$Q_{\text{recha}}$  at  $x = 1/3$  should be  $0 \text{ mAh g}^{-1}$ , because all the Mn ions are in the 4+ state. The  $Q_{\text{recha}}$  value for the  $x = 1/3$  sample is, however, about  $45 \text{ mAh g}^{-1}$ . This is caused by the presence of the  $\text{Li}_2\text{MnO}_3$  impurity as illustrated in Figs. 1 and 2. The  $W(\text{Li}_2\text{MnO}_3)$  value is almost consistent with the result of electrochemical charge and discharge tests, because the  $Q_{\text{recha}}$  value for the rest of spinel phase, i.e.  $\text{Li}[\text{Li}_{0.21}\text{Mn}_{1.79}]\text{O}_4$  is calculated to be  $\sim 56 \text{ mAh g}^{-1}$ . However, it should be noted that our recent muon-spin rotation/relaxation ( $\mu\text{SR}$ ) study on the  $x = 1/3$  compound reveals that the distribution of  $\text{Li}^+$  ions at the 16d site is microscopically inhomogeneous [24]. Here,  $\mu\text{SR}$  is very sensitive to local magnetic environment and is an effective technique for investigating the (volume) fraction of each different phase in a sample.

### 3.3. Coefficients of thermal expansion for $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$

Fig. 4 shows the  $T$  dependence of cubic lattice parameter ( $a_c$ ) and orthorhombic lattice parameters ( $a_0$ ,  $b_0$ , and  $c_0$ ) for the LMO samples with (a)  $x = 0$  and (b)  $x = 0.05, 0.1, 0.15, 0.2$ , and  $1/3$ . As  $T$  decreases from 400 K,  $a_c$  for the  $x = 0$  sample decreases almost linearly down to 300 K, and then separates into the three orthorhombic lattice parameters of  $a_0$ ,  $b_0$ , and  $c_0$  at 282.5 K ( $=T_{\text{JT}}$ ) due to the cooperative JT transition. The present  $T_{\text{JT}}$  is almost comparable with the magnetic anomalies in the susceptibility ( $\chi$ ) at 290 K [32]



**Fig. 4.** Temperature ( $T$ ) dependence of cubic lattice parameter ( $a_c$ ) and orthorhombic lattice parameters ( $a_o$ ,  $b_o$ , and  $c_o$ ) for the  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  samples with (a)  $x = 0$  and (b)  $x = 0.05, 0.1, 0.15, 0.2$ , and  $1/3$ .  $T_{\text{JT}}$ ,  $c$ , and  $o$  stand for the  $T$  of the cooperative Jahn–Teller (JT) transition, cubic, and orthorhombic, respectively. The lattice parameters of  $a_c$  and  $c_o$  for the  $x = 0$  sample are multiplied by three for comparison.

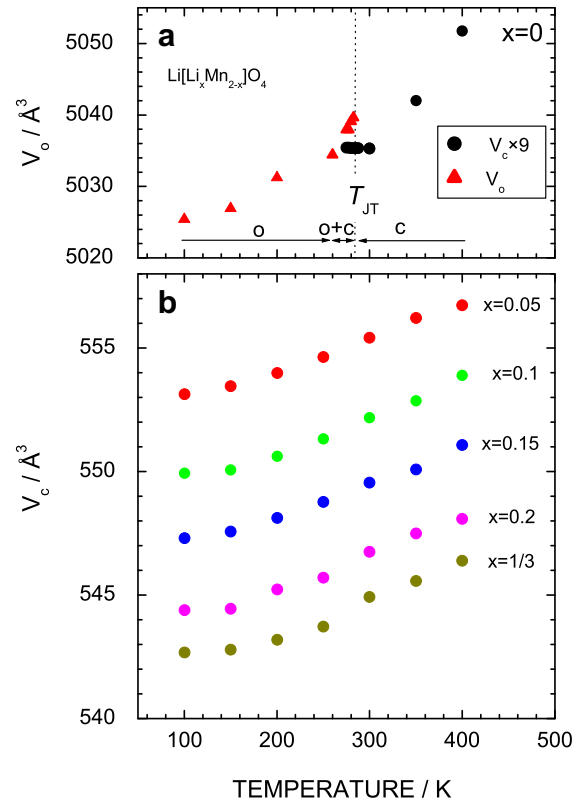
and  $\mu\text{SR}$  measurements at 280 K [33]. Note that the cubic phase for the  $x = 0$  sample is observed even below  $T_{\text{JT}}$ ; a mixture of the cubic phase ( $Fd\bar{3}m$ ) and the orthorhombic phase ( $Fddd$ ) is stable in the  $T$  range between 282.5 and 270 K, whereas the single orthorhombic phase ( $Fddd$ ) appears below 250 K. This is due to the phase transition of the first kind as probed by a differential scanning calorimetry (DSC) [17]. For the samples with  $x \geq 0.05$ , the  $a_c$  values decrease almost linearly down to  $\sim 200$  K, then decrease with changing the slope ( $da_c/dT$ ) with further decreasing  $T$ .

As shown in Fig. 5(a), the lattice volume for the  $x = 0$  sample indicates discontinuous  $T$  dependence at  $T_{\text{JT}}$ . That is, as  $T$  decreases from 400 K,  $V_o$  for the  $x = 0$  sample decreases almost linearly down to  $\sim 300$  K, then slightly increases at 282.5 K, and finally decreases linearly with further lowering  $T$ . Since  $V_c = 5035.3(1) \text{ \AA}^3$  at 285 K and  $V_o = 5039.6(1) \text{ \AA}^3$  at 282.5 K, about 0.1% of volume expansion occurs at the JT transition. This means that the crystal lattice of  $x = 0$  undergoes the abrupt volume change near the room  $T$  without changing the Li composition. Here, although the  $x = 0$  sample is in the single cubic phase ( $Fd\bar{3}m$ ) above 300 K, the  $V_c$  value is converted into the  $V_o$  value ( $V_o/V_c \times 9$ ) for comparison. For the samples with  $x \geq 0.05$ , the  $T$  dependence of  $V_c$  is similar to that of  $a_c$  (see Fig. 5(b)).

The average coefficient of linear thermal expansion ( $\alpha_L$ ) at 300 K is calculated as follow:

$$\alpha_L = \frac{\Delta l}{\Delta T \times l(300 \text{ K})}, \quad (3)$$

where  $l$  is the length of lattice parameter such as  $a_c$  and  $a_o$ , and  $l(300 \text{ K})$  is the  $l$  at 300 K [ $l(285 \text{ K})$  is used only for the  $x = 0$  sample]. As shown in Fig. 6(a), the  $\alpha_L$  values for the  $x = 0$  sample are quite different between the three orthorhombic axes, that is,



**Fig. 5.** Temperature ( $T$ ) dependence of cubic lattice volume ( $V_c$ ) and orthorhombic lattice volume ( $V_o$ ) for the  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  samples with (a)  $x = 0$  and (b)  $x = 0.05, 0.1, 0.15, 0.2$ , and  $1/3$ .  $T_{\text{JT}}$ ,  $c$ , and  $o$  stand for the  $T$  of the cooperative Jahn–Teller (JT) transition, cubic, and orthorhombic, respectively. The cubic lattice volume of  $V_c$  for the  $x = 0$  sample is multiplied by nine for comparison.

$\alpha_L = 1.3(1) \times 10^{-6} \text{ K}^{-1}$  along the  $a_o$ -axis,  $\alpha_L = 13.1(1) \times 10^{-6} \text{ K}^{-1}$  along the  $b_o$ -axis, and  $\alpha_L = 5.7(1) \times 10^{-6} \text{ K}^{-1}$  along the  $c_o$ -axis. In contrast to the linear decrease in  $a_c$  with increasing  $x$ ,  $\alpha_L$  for the samples with  $x \geq 0.05$  ranges  $7.2\text{--}8.0 \times 10^{-6} \text{ K}^{-1}$  (see Fig. 6(b)). Moreover, the  $\alpha_L$  value which is calculated in the  $T$  range between 100 and 300 K shows similar  $x$  dependence.

For a cubic phase, the average coefficient of volumetric thermal expansion ( $\beta_V$ ) can be calculated by  $\beta_V = 3 \times \alpha_L$  assuming the isotropic expansion. Since the  $x = 0$  sample is in the orthorhombic phase ( $Fddd$ ) below 285 K,  $\beta_V$  is calculated as follow for comparison:

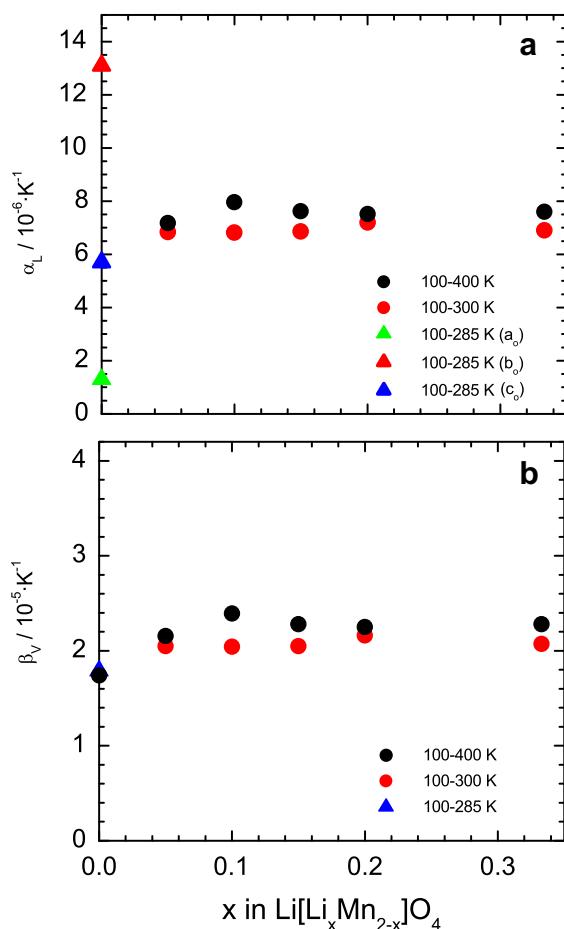
$$\beta_V = \frac{\Delta V}{\Delta T \times V(300 \text{ K})}, \quad (4)$$

where  $V$  is the volume and  $V(300 \text{ K})$  is the  $V$  at 300 K. Fig. 6(b) shows the  $x$  dependence of  $\beta_V$  for the LMO samples. In contrast to anisotropic thermal expansion along the three orthorhombic axes,  $\beta_V$  for the  $x = 0$  sample does not change between the  $T$  ranges;  $\beta_V = 1.79(1) \times 10^{-5} \text{ K}^{-1}$  at 100–285 K and  $\beta_V = 1.74(1) \times 10^{-5} \text{ K}^{-1}$  at 100–400 K. For the samples with  $x \geq 0.05$ ,  $\beta_V$  is almost independent of  $x$  as in the case for  $\alpha_L$ .

#### 4. Discussion

Table 1 summarizes the  $\alpha_L$  and  $\beta_V$  values for the LMO samples. For the  $x = 0$  sample, it is interesting to note that the  $\alpha_L$  value of  $a_o$ -axis is quite small compared to that of  $c_o$ -axis, because  $a_o$  is longer than  $c_o$ . This can be understood by another phase transition below 100 K, that is, an antiferromagnetic (AF) transition with  $T_N = 60 \text{ K}$  [18,20,33]. Fig. 7 shows the schematic illustration of the crystal





**Fig. 6.** Average coefficients of (a) linear thermal expansion ( $\alpha_L$ ) and (b) volumetric thermal expansion ( $\beta_V$ ) for the  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  samples with  $0 \leq x \leq 1/3$ .

structure of  $x = 0$  in the orthorhombic phase ( $Fddd$ ). Both  $\text{Mn}^{3+}$  spins with  $S = 2$  ( $t_{2g}^3 e_g^1$ ) and  $\text{Mn}^{4+}$  spins with  $S = 3/2$  ( $t_{2g}^3$ ) are coupled in the antiparallel mode (up and down) in the AF phase. Since the  $\text{Mn}^{3+}/\text{Mn}^{4+}$  arrangement of  $a_0$ -axis is same to that of  $b_0$ -axis, the small decrease in  $a_0$  with decreasing  $T$  stabilizes the charge ordering of  $\text{Mn}^{3+}/\text{Mn}^{4+}$  ions. In other words, the AF order is

**Table 1**

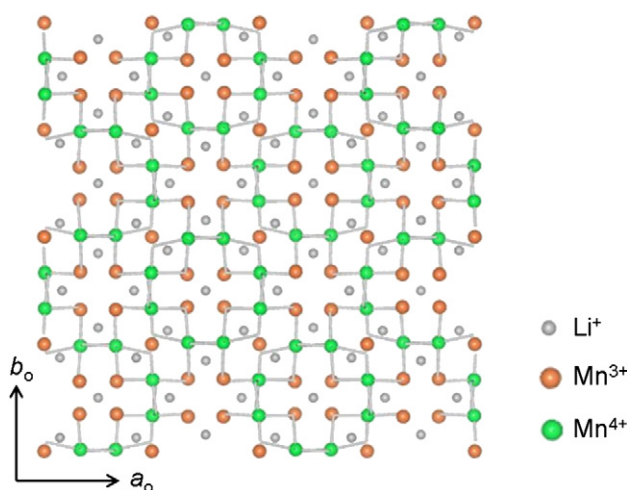
Average linear thermal expansion ( $\alpha_L$ ) and volumetric thermal expansion ( $\beta_V$ ) for the  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  samples with  $0 \leq x \leq 1/3$  together with those for other lithium-ion battery materials.

Sample	$\alpha_L/10^{-6} \text{ K}^{-1}$	$\beta_V/10^{-5} \text{ K}^{-1}$	Range/K	Reference
$x = 0^a$	1.3(1) ( $a_0$ ) 13.1(1) ( $b_0$ ) 5.7(1) ( $c_0$ )	1.74(1)	100–400	This work
$x = 0.05$	6.84(1)	2.16(1)	100–400	This work
$x = 0.1$	7.11(1)	2.39(1)	100–400	This work
$x = 0.15$	6.86(1)	2.28(1)	100–400	This work
$x = 0.2$	7.21(1)	2.25(1)	100–400	This work
$x = 1/3^b$	6.94(1)	2.28(1)	100–400	This work
$\text{LiV}_2\text{O}_4$	7.29	2.18	5–300	[36]
$\text{Fe}[\text{Li}_{1/2}\text{Fe}_{3/2}]\text{O}_4$	3.15	0.94	10–300	[37]
$\text{LiCoO}_2^c$	12.7 ( $a_h$ ) 15.7 ( $c_h$ )	4.13(1)	90–300	[7]
$\text{Li}_{0.6}\text{CoO}_2^c$	10.6 ( $a_h$ ) 44.3 ( $c_h$ )	5.36(1)	90–300	[7]

<sup>a</sup> The  $\alpha_L$  values are calculated in the temperature range between 100 and 285 K.

<sup>b</sup> The crystal structure is a mixture of the cubic spinel phase and the monoclinic  $\text{Li}_2\text{MnO}_3$  phase.

<sup>c</sup> The lattice parameters are calculated in hexagonal setting.



**Fig. 7.** Schematic illustration of the crystal structure of  $\text{LiMn}_2\text{O}_4$  in the orthorhombic phase ( $Fddd$ ). Although  $a_0$  is smaller than  $b_0$  down to 100 K, the  $\text{Mn}^{3+}/\text{Mn}^{4+}$  arrangement of  $a_0$ -axis is same to that of  $b_0$ -axis.

thought to be correlated with the anisotropic thermal expansion between the three orthorhombic lattice parameters.

The electrochemical measurements indicate that the partial substitution of Li ions at the 16d site improves the cycleability of charge and discharge reactions (see Fig. 3). This is consistent with the previous results on  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  [28] and  $\text{Li}[\text{M}_x\text{Mn}_{2-x}]\text{O}_4$  ( $M = \text{Cr}, \text{Co}, \text{and Ni}$ ) [34]. Although the authors in Refs. [28,34] explain that the improvement of their cycleability is caused by the strengthening of the bonds between the cation and  $\text{O}^{2-}$  ions, as  $x$  increases from 0,  $\beta_V$  slightly increases up to  $x = 0.05$ , and then keeps constant value ( $\sim 2.2 \times 10^{-5} \text{ K}^{-1}$ ) with further increasing  $x$  (see Table 1). This suggests that the bond strength between the  $\text{Mn}(\text{Li})$  and  $\text{O}^{2-}$  ions does not increase by the partial substitution for Mn ions. Since our  $\mu\text{SR}$  measurements demonstrate that the local JT distortion exists even for the  $x = 0.15$  composition [33], the excellent cycleability for the samples with  $x \geq 0.05$  is attributed to the inhibition of formation of double hexagonal phase around 4.5 V and/or dissolution of Mn ions.

The XRD density ( $d_{\text{XRD}}$ ) at 300 K linearly decreases with increasing  $x$ , for example,  $d_{\text{XRD}} = 4.293(1) \text{ g cm}^{-3}$  for  $x = 0$ ,  $d_{\text{XRD}} = 4.236(1) \text{ g cm}^{-3}$  for  $x = 0.1$ , and  $d_{\text{XRD}} = 4.160(1) \text{ g cm}^{-3}$  for  $x = 0.2$ . The  $x$  dependences of  $\alpha_L$  and  $\beta_V$  show that the thermal expansion for LMO has no direct relation with  $d_{\text{XRD}}$ . This consideration is also supported by the facts that  $\alpha_L$  for  $\text{MgAl}_2\text{O}_4$  with  $d_{\text{XRD}} = 3.58 \text{ g cm}^{-3}$  is almost the same ( $\sim 9 \times 10^{-6} \text{ K}^{-1}$ ) to that for  $\text{Co}_3\text{O}_4$  with  $d_{\text{XRD}} = 6.05 \text{ g cm}^{-3}$  [35].

Comparing with other lithium battery materials, the  $\alpha_L$  (or  $\beta_V$ ) values for the LMO samples are almost similar to that for  $\text{LiV}_2\text{O}_4$  [36] and about two times larger than that for  $\text{Fe}[\text{Li}_{1/2}\text{Fe}_{3/2}]\text{O}_4$  [37]. Furthermore, the  $\alpha_L$  values for  $\text{LiCoO}_2$  and  $\text{Li}_{0.6}\text{CoO}_2$  [7] are 2–6 times larger than those for LMO. From the view points of  $\alpha_L$  and  $\beta_V$ , LMO is found to be suitable for the electrode materials for all solid-state LIB. If we assume that the operating  $T$  width of all solid-state LIB is 100 K centered at room  $T$  ( $-30^\circ \text{C} \leq T \leq 70^\circ \text{C}$ ), the maximum volume change induced by the thermal difference is estimated as about 0.2% for all the LMO samples.

## 5. Conclusion

The coefficients of thermal expansion (CTE) in lithium manganese oxide spinels  $\text{Li}[\text{Li}_x\text{Mn}_{2-x}]\text{O}_4$  (LMO) were investigated by X-ray diffraction measurements. As  $x$  increases from 0, the average volumetric thermal expansion ( $\beta_V$ ) slightly increases up to  $x = 0.05$ ,

and then levels off at constant value ( $\sim 2.2 \times 10^{-5} \text{ K}^{-1}$ ) with further increasing  $x$ . This suggests that the bond strength between Mn(Li) and  $\text{O}^{2-}$  ions does not increase by the partial substitution of Li ions for Mn ions. The CTE values are effective to know the optimum conditions for all solid-state lithium-ion battery, because the solid–solid interface is usually constructed by heat treatment. Although we focused on the CTE for LMO in the present work, such studies on other lithium insertion materials together with their delithiated states are progress in our laboratory.

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